## NAME

CEH - CUTEr tool to evaluate the sparse Lagrangian Hessian matrix in finite element format.

By convention, the signs of the Lagrange multipliers V are set so the Lagrangian function can be written as $L(X, V)=f(X)+\langle c(X), V\rangle$.

## SYNOPSIS

CALL CEH( N, M, X, LV, V, NE, IRNHI, LIRNHI, LE, IPRNHI, HI, LHI, IPRHI, BYROWS )
DESCRIPTION
The CEH subroutine evaluates the Hessian matrix of the Lagrangian function for the problem decoded into OUTSDIF.d at the point X in the constrained minimization case. This Hessian matrix is stored as a sparse matrix in finite element format
$\mathrm{H}=$ sum $\mathrm{H} \_\mathrm{i} \quad(\mathrm{i}=1, \ldots, \mathrm{NE})$,
where each square symmetric element H_i involves a small subset of the rows of the Hessian matrix.

## ARGUMENTS

The arguments of CEH are as follows
$\mathbf{N}$ [in] - integer
the number of variables for the problem,
$\mathbf{M}$ [in] - integer
the total number of general constraints,
$\mathbf{X}$ [in] - real/double precision
an array which gives the current estimate of the solution of the problem,
$\mathbf{L V}$ [in] - integer
the actual declared dimension of V ,
V [in] - real/double precision
an array which gives the Lagrange multipliers,
NE [out] - integer
the number, ne, of "finite-elements" used,
IRNHI [out] - integer
an array which holds a list of the row indices involved which each element. Those for element i directly preceed those for element $i+1, i=1, \ldots$, NE- 1 . Since the elements are symmetric, IRNHI is also the list of column indices involved with each element.

LIRNHI [in] - integer
the actual declared dimension of IRNHI,
$\mathbf{L E}$ [in] - integer
the actual declared dimensions of IPRNHI and IPRHI,
IPRNHI [out] - integer
IPRNHI(i) points to the position in IRNHI of the first row index involved with element number i: the row indices of element number i are stored in IRNHI between the indices IPRNHI(i) and IPRNHI(i+1)-1. IPRNHI(NE+1) points to the first empty location in IRNHI,

HI [out] - real/double precision
an array of the nonzeros in the upper triangle of $\mathrm{H}_{-} \mathrm{i}$, evaluated at X and stored by rows, or by columns. Those for element i directly proceed those for element, $\mathrm{i}+1, \mathrm{i}=1, \ldots, \mathrm{NE}-1$. Element number i contains the values stored between

HI( IPRHI(i) ) and HI( IPRHI(i+1)-1 )
and involves the rows/columns stored between

IRNHI( IPRNHI(i) ) and IRNHI( IPRNHI(i+1)-1 ).
LHI [in] - integer
the actual declared dimension of HI ,
IPRHI [out] - integer
$\operatorname{IPRHI}(\mathrm{i})$ points to the position in HI of the first nonzero involved with element number i: the values involved in element number i are stored in HI between the indices $\operatorname{IPRHI}(\mathrm{i})$ and $\operatorname{IPRHI}(\mathrm{i}+1)-1$. $\operatorname{IPRHI}(\mathrm{NE}+1)$ points to the fi rst empty location in HI ,

BYROWS [in] - logical
must be set to .TRUE. if the upper triangle of each $\mathrm{H}_{-}$i is to be stored by rows, and to .FALSE. if it is to be stored by columns.

## AUTHORS

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## SEE ALSO

CUTEr (and SifDec): A Constrained and Unconstrained Testing Environment, revisited, N.I.M. Gould, D. Orban and Ph.L. Toint, ACM TOMS, 29:4, pp.373-394, 2003.

CUTE: Constrained and Unconstrained Testing Environment, I. Bongartz, A.R. Conn, N.I.M. Gould and Ph.L. Toint, TOMS, 21:1, pp.123-160, 1995.
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